**Georgia**

**Standards of Excellence**

**Course Curriculum Overview**

**Mathematics**

GSE Geometry



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| **GSE Geometry Curriculum Map** | | | | | |
| **1st Semester** | | | **2nd Semester** | | |
|  |  |  |  |  |  |
| **Unit 1**  ***(2 –3 weeks)*** | **Unit 2**  ***(9 – 10 weeks)*** | **Unit 3**  ***(3 – 4 weeks)*** | **Unit 4**  ***(6 – 7 weeks)*** | **Unit 5**  ***(4 – 5 weeks)*** | **Unit 6**  ***(4 – 5 weeks)*** |
| **Transformations in the Coordinate Plane** | **Similarity, Congruence, and Proofs** | **Right Triangle Trigonometry** | **Circles and Volume** | **Geometric and Algebraic Connections** | **Applications of Probability** |
| **MGSE9-12.G.CO.1**  **MGSE9-12.G.CO.2 MGSE9-12.G.CO.3 MGSE9-12.G.CO.4 MGSE9-12.G.CO.5** | **MGSE9-12.G.SRT.1**  **MGSE9-12.G.SRT.2**  **MGSE9-12.G.SRT.3**  **MGSE9-12.G.SRT.4**  **MGSE9-12.G.SRT.5**  **MGSE9-12.G.CO.6**  **MGSE9-12.G.CO.7**  **MGSE9-12.G.CO.8**  **MGSE9-12.G.CO.9**  **MGSE9-12.G.CO.10**  **MGSE9-12.G.CO.11**  **MGSE9-12.G.CO.12**  **MGSE9-12.G.CO.13** | **MGSE9-12.G.SRT.6**  **MGSE9-12.G.SRT.7**  **MGSE9-12.G.SRT.8** | **MGSE9-12.G.C.1**  **MGSE9-12.G.C.2**  **MGSE9-12.G.C.3**  **MGSE9-12.G.C.4**  **MGSE9-12.G.C.5**  **MGSE9-12.G.GMD.1**  **MGSE9-12.G.GMD.2**  **MGSE9-12.G.GMD.3**  **MGSE9-12.G.GMD.4** | **MGSE9-12.G.GPE.1**  **MGSE9-12.G.GPE.4**  **MGSE9-12.G.GPE.5**  **MGSE9-12.G.GPE.6**  **MGSE9-12.G.GPE.7**  **MGSE9-12.G.MG.1**  **MGSE9-12.G.MG.2**  **MGSE9-12.G.MG.3** | **MGSE9-12.S.CP.1**  **MGSE9-12.S.CP.2**  **MGSE9-12.S.CP.3**  **MGSE9-12.S.CP.4**  **MGSE9-12.S.CP.5**  **MGSE9-12.S.CP.6**  **MGSE9-12.S.CP.7** |
|  |  |  |  |  |  |
| These units were written to build upon concepts from prior units, so later units contain tasks that depend upon the concepts addressed in earlier units.  All units will include the Mathematical Practices and indicate skills to maintain. | | | | | |

**NOTE:** Mathematical standards are interwoven and should be addressed throughout the year in as many different units and tasks as possible in order to stress the natural connections that exist among mathematical topics.

**Grade 9-12 Key:**

**Number and Quantity Strand:** RN = The Real Number System, Q = Quantities, CN = Complex Number System, VM = Vector and Matrix Quantities

**Algebra Strand:** SSE = Seeing Structure in Expressions, APR = Arithmetic with Polynomial and Rational Expressions, CED = Creating Equations, REI = Reasoning with Equations and Inequalities

**Functions Strand:** IF = Interpreting Functions, LE = Linear and Exponential Models, BF = Building Functions, TF = Trigonometric Functions

**Geometry Strand:** CO = Congruence, SRT = Similarity, Right Triangles, and Trigonometry, C = Circles, GPE = Expressing Geometric Properties with Equations, GMD = Geometric Measurement and Dimension,

MG = Modeling with Geometry

**Statistics and Probability Strand:** ID = Interpreting Categorical and Quantitative Data, IC = Making Inferences and Justifying Conclusions, CP = Conditional Probability and the Rules of Probability, MD = Using Probability to Make Decisions

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The Comprehensive Course Overviews are designed to provide access to multiple sources of support for implementing and instructing courses involving the Georgia Standards of Excellence.

# GSE Geometry

**Geometry** is the second course in a sequence of three required high school courses designed to ensure career and college readiness. The course represents a discrete study of geometry with correlated statistics applications.

The standards in the three-course high school sequence specify the mathematics that all students should study in order to be college and career ready. Additional mathematics content is provided in fourth credit courses and advanced courses including pre-calculus, calculus, advanced statistics, discrete mathematics, and mathematics of finance courses. High school course content standards are listed by conceptual categories including Number and Quantity, Algebra, Functions, Geometry, and Statistics and Probability. Conceptual categories portray a coherent view of high school mathematics content; a student’s work with functions, for example, crosses a number of traditional course boundaries, potentially up through and including calculus. Standards for Mathematical Practice provide the foundation for instruction and assessment.

# GSE Geometry: Unit Descriptions

**Unit 1**: Building on standards from middle school, students will perform transformations in the coordinate plane, describe a sequence of transformations that will map one figure onto another, and describe transformations that will map a figure onto itself. Students will compare transformations that preserve distance and angle to those that do not.

**Unit 2**: Building on standards from Unit 1 and from middle school, students will use transformations and proportional reasoning to develop a formal understanding of similarity and congruence. Students will identify criteria for similarity and congruence of triangles, develop facility with geometric proofs (variety of formats), and use the concepts of similarity and congruence to prove theorems involving lines, angles, triangles, and other polygons.

**Unit 3**: Students will apply similarity in right triangles to understand right triangle trigonometry. Students will use the Pythagorean Theorem and the relationship between the sine and cosine of complementary angles to solve problems involving right triangles.

**Unit 4**: Students will understand and apply theorems about circles, find arc lengths of circles, and find areas of sectors of circles. Students will develop and explain formulas related to circles and the volume of solid figures and use the formulas to solve problems. Building on standards from middle school, students will extend the study of identifying cross-sections of three-dimensional shapes to identifying three-dimensional objects generated by rotations of two-dimensional objects.

**Unit 5**: Students will use the concepts of distance, midpoint, and slope to verify algebraically geometric relationships of figures in the coordinate plane (triangles, quadrilaterals, and circles). Students will solve problems involving parallel and perpendicular lines, perimeters and areas of polygons, and the partitioning of a segment in a given ratio. Students will derive the equation of a circle and model real-world objects using geometric shapes and concepts.

**Unit 6**: Students will understand independence and conditional probability and use them to interpret data. Building on standards from middle school, students will formalize the rules of probability and use the rules to compute probabilities of compound events in a uniform probability model.

# Flipbooks

These “FlipBooks” were developed by the Kansas Association of Teachers of Mathematics (KATM) and are a compilation of research, “unpacked” standards from many states, instructional strategies and examples for each standard at each grade level. The intent is to show the connections to the Standards of Mathematical Practices for the content standards and to get detailed information at each level. The [**High School Flipbook**](http://ccgpsmathematics9-10.wikispaces.com/KATM+Flipbook)is an interactive document arranged by the content domains listed on the following pages. The links on each domain and standard will take you to specific information on that standard/domain within the Flipbook.

# Mathematics | High School – Geometry

An understanding of the attributes and relationships of geometric objects can be applied in diverse contexts—interpreting a schematic drawing, estimating the amount of wood needed to frame a sloping roof, rendering computer graphics, or designing a sewing pattern for the most efficient use of material.

Although there are many types of geometry, school mathematics is devoted primarily to plane Euclidean geometry, studied both synthetically (without coordinates) and analytically (with coordinates). Euclidean geometry is characterized most importantly by the Parallel Postulate that states that through a point not on a given line there is exactly one parallel line. (Spherical geometry, in contrast, has no parallel lines.) During high school, students begin to formalize their geometry experiences from elementary and middle school, using more precise definitions and developing careful proofs. Later in college some students develop Euclidean and other geometries carefully from a small set of axioms.

The concepts of congruence, similarity, and symmetry can be understood from the perspective of geometric transformation. Fundamental are the rigid motions: translations, rotations, reflections, and combinations of these, all of which are here assumed to preserve distance and angles (and therefore shape in general). Reflections and rotations each explain a particular type of symmetry, and the symmetries of an object offer insight into its attributes—as when the reflective symmetry of an isosceles triangle assures that its base angles are congruent.

In the approach taken here, two geometric figures are defined to be congruent if there is a sequence of rigid motions that carries one onto the other. This is the principle of superposition. For triangles, congruence means the equality of all corresponding pairs of sides and all corresponding pairs of angles. During the middle grades, through experiences drawing triangles from given conditions, students notice ways to specify enough measures in a triangle to ensure that all triangles drawn with those measures are congruent. Once these triangle congruence criteria (ASA, SAS, and SSS) are established using rigid motions, they can be used to prove theorems about triangles, quadrilaterals, and other geometric figures.

Similarity transformations (rigid motions followed by dilations) define similarity in the same way that rigid motions define congruence, thereby formalizing the similarity ideas of "same shape" and "scale factor" developed in the middle grades. These transformations lead to the criterion for triangle similarity that two pairs of corresponding angles are congruent.

The definitions of sine, cosine, and tangent for acute angles are founded on right triangles and similarity, and, with the Pythagorean Theorem, are fundamental in many real-world and theoretical situations. The Pythagorean Theorem is generalized to non-right triangles by the Law of Cosines. Together, the Laws of Sines and Cosines embody the triangle congruence criteria for the cases where three pieces of information suffice to completely solve a triangle. Furthermore, these laws yield two possible solutions in the ambiguous case, illustrating that Side-Side-Angle is not a congruence criterion.

**Connections to Equations.** The correspondence between numerical coordinates and geometric points allows methods from algebra to be applied to geometry and vice versa. The solution set of an equation becomes a geometric curve, making visualization a tool for doing and understanding algebra. Geometric shapes can be described by equations, making algebraic manipulation into a tool for geometric understanding, modeling, and proof.

**Congruence G.CO**

**Experiment with transformations in the plane**

**MGSE9-12.G.CO.1** Know precise definitions of angle, circle, perpendicular line, parallel line, and line segment, based on the undefined notions of point, line, distance along a line, and distance around a circular arc.

**MGSE9-12.G.CO.2** Represent transformations in the plane using, e.g., transparencies and geometry software; describe transformations as functions that take points in the plane as inputs and give other points as outputs. Compare transformations that preserve distance and angle to those that do not (e.g., translation versus horizontal stretch).

**MGSE9-12.G.CO.3** Given a rectangle, parallelogram, trapezoid, or regular polygon, describe the rotations and reflections that carry it onto itself.

**MGSE9-12.G.CO.4** Develop definitions of rotations, reflections, and translations in terms of angles, circles, perpendicular lines, parallel lines, and line segments.

**MGSE9-12.G.CO.5** Given a geometric figure and a rotation, reflection, or translation, draw the transformed figure using, e.g., graph paper, tracing paper, or geometry software. Specify a sequence of transformations that will carry a given figure onto another.

**Understand congruence in terms of rigid motions**

**MGSE9-12.G.CO.6** Use geometric descriptions of rigid motions to transform figures and to predict the effect of a given rigid motion on a given figure; given two figures, use the definition of congruence in terms of rigid motions to decide if they are congruent.

**MGSE9-12.G.CO.7** Use the definition of congruence in terms of rigid motions to show that two triangles are congruent if and only if corresponding pairs of sides and corresponding pairs of angles are congruent.

**MGSE9-12.G.CO.8** Explain how the criteria for triangle congruence (ASA, SAS, and SSS) follow from the definition of congruence in terms of rigid motions. (Extend to include HL and AAS.)

**Prove geometric theorems**

**MGSE9-12.G.CO.9** Prove theorems about lines and angles. Theorems include: vertical angles are congruent; when a transversal crosses parallel lines, alternate interior angles are congruent and corresponding angles are congruent; points on a perpendicular bisector of a line segment are exactly those equidistant from the segment’s endpoints.

**MGSE9-12.G.CO.10** Prove theorems about triangles. Theorems include: measures of interior angles of a triangle sum to 180 degrees; base angles of isosceles triangles are congruent; the segment joining midpoints of two sides of a triangle is parallel to the third side and half the length; the medians of a triangle meet at a point.

**MGSE9-12.G.CO.11** Prove theorems about parallelograms. Theorems include: opposite sides are congruent, opposite angles are congruent, the diagonals of a parallelogram bisect each other, and conversely, rectangles are parallelograms with congruent diagonals.

**Make geometric constructions**

**MGSE9-12.G.CO.12** Make formal geometric constructions with a variety of tools and methods (compass and straightedge, string, reflective devices, paper folding, dynamic geometric software, etc.). Copying a segment; copying an angle; bisecting a segment; bisecting an angle; constructing perpendicular lines, including the perpendicular bisector of a line segment; and constructing a line parallel to a given line through a point not on the line.

**MGSE9-12.G.CO.13** Construct an equilateral triangle, a square, and a regular hexagon, each inscribed in a circle.

**Similarity, Right Triangles, and Trigonometry G.SRT**

**Understand similarity in terms of similarity transformations**

**MGSE9-12.G.SRT.1** Verify experimentally the properties of dilations given by a center and a scale factor.

1. The dilation of a line not passing through the center of the dilation results in a parallel line and leaves a line passing through the center unchanged.
2. The dilation of a line segment is longer or shorter according to the ratio given by the scale factor.

**MGSE9-12.G.SRT.2** Given two figures, use the definition of similarity in terms of similarity transformations to decide if they are similar; explain, using similarity transformations, the meaning of similarity for triangles as the equality of all corresponding pairs of angles and the proportionality of all corresponding pairs of sides.

**MGSE9-12.G.SRT.3** Use the properties of similarity transformations to establish the AA criterion for two triangles to be similar.

**Prove theorems involving similarity**

**MGSE9-12.G.SRT.4** Prove theorems about triangles. Theorems include: a line parallel to one side of a triangle divides the other two proportionally, (and its converse); the Pythagorean Theorem using triangle similarity.

**MGSE9-12.G.SRT.5** Use congruence and similarity criteria for triangles to solve problems and to prove relationships in geometric figures.

**Define trigonometric ratios and solve problems involving right triangles**

**MGSE9-12.G.SRT.6** Understand that by similarity, side ratios in right triangles are properties of the angles in the triangle, leading to definitions of trigonometric ratios for acute angles.

**MGSE9-12.G.SRT.7** Explain and use the relationship between the sine and cosine of complementary angles.

**MGSE9-12.G.SRT.8** Use trigonometric ratios and the Pythagorean Theorem to solve right triangles in applied problems.

**Circles G.C**

**Understand and apply theorems about circles**

**MGSE9-12.G.C.1** Understand that all circles are similar.

**MGSE9-12.G.C.2** Identify and describe relationships among inscribed angles, radii, chords, tangents, and secants. Include the relationship between central, inscribed, and circumscribed angles; inscribed angles on a diameter are right angles; the radius of a circle is perpendicular to the tangent where the radius intersects the circle.

**MGSE9-12.G.C.3** Construct the inscribed and circumscribed circles of a triangle, and prove properties of angles for a quadrilateral inscribed in a circle.

**MGSE9-12.G.C.4** Construct a tangent line from a point outside a given circle to the circle.

**Find arc lengths and areas of sectors of circles**

**MGSE9-12.G.C.5** Derive using similarity the fact that the length of the arc intercepted by an angle is proportional to the radius, and define the radian measure of the angle as the constant of proportionality; derive the formula for the area of a sector.

**Expressing Geometric Properties with Equations G.GPE**

**Translate between the geometric description and the equation for a conic section**

**MGSE9-12.G.GPE.1** Derive the equation of a circle of given center and radius using the Pythagorean Theorem; complete the square to find the center and radius of a circle given by an equation.

**Use coordinates to prove simple geometric theorems algebraically**

**MGSE9-12.G.GPE.4** Use coordinates to prove simple geometric theorems algebraically.  *For example, prove or disprove that a figure defined by four given points in the coordinate plane is a rectangle; prove or disprove that the point (1, √3) lies on the circle centered at the origin and containing the point (0,2).*

(Focus on quadrilaterals, right triangles, and circles.)

**MGSE9-12.G.GPE.5** Prove the slope criteria for parallel and perpendicular lines and use them to solve geometric problems (e.g., find the equation of a line parallel or perpendicular to a given line that passes through a given point).

**MGSE9-12.G.GPE.6** Find the point on a directed line segment between two given points that partitions the segment in a given ratio.

**MGSE9-12.G.GPE.7** Use coordinates to compute perimeters of polygons and areas of triangles and rectangles, e.g., using the distance formula.

**Geometric Measurement and Dimension G.GMD**

**Explain volume formulas and use them to solve problems**

**MGSE9-12.G.GMD.1** Give informal arguments for geometric formulas.

1. Give informal arguments for the formulas of the circumference of a circle and area of a circle using dissection arguments and informal limit arguments.
2. Give informal arguments for the formula of the volume of a cylinder, pyramid, and cone using Cavalieri’s principle.

**MGSE9-12.G.GMD.2** Give an informal argument using Cavalieri’s principle for the formulas for the volume of a sphere and other solid figures.

**MGSE9-12.G.GMD.3** Use volume formulas for cylinders, pyramids, cones, and spheres to solve problems.

**Visualize relationships between two-dimensional and three-dimensional objects**

**MGSE9-12.G.GMD.4** Identify the shapes of two-dimensional cross-sections of three-dimensional objects, and identify three-dimensional objects generated by rotations of two-dimensional objects.

**Modeling with Geometry G.MG**

**Apply geometric concepts in modeling situations**

**MGSE9-12.G.MG.1** Use geometric shapes, their measures, and their properties to describe objects

(e.g., modeling a tree trunk or a human torso as a cylinder).

**MGSE9-12.G.MG.2** Apply concepts of density based on area and volume in modeling situations

(e.g., persons per square mile, BTUs per cubic foot).

**MGSE9-12.G.MG.3** Apply geometric methods to solve design problems (e.g., designing an object or structure to satisfy physical constraints or minimize cost; working with typographic grid systems based on ratios).

Mathematics | High School—Statistics and Probability

Decisions or predictions are often based on data—numbers in context. These decisions or predictions would be easy if the data always sent a clear message, but the message is often obscured by variability. Statistics provides tools for describing variability in data and for making informed decisions that take it into account.

Data are gathered, displayed, summarized, examined, and interpreted to discover patterns and deviations from patterns. Quantitative data can be described in terms of key characteristics: measures of shape, center, and spread. The shape of a data distribution might be described as symmetric, skewed, flat, or bell shaped, and it might be summarized by a statistic measuring center (such as mean or median) and a statistic measuring spread (such as standard deviation or interquartile range). Different distributions can be compared numerically using these statistics or compared visually using plots. Knowledge of center and spread are not enough to describe a distribution. Which statistics to compare, which plots to use, and what the results of a comparison might mean, depend on the question to be investigated and the real-life actions to be taken.

Randomization has two important uses in drawing statistical conclusions. First, collecting data from a random sample of a population makes it possible to draw valid conclusions about the whole population, taking variability into account. Second, randomly assigning individuals to different treatments allows a fair comparison of the effectiveness of those treatments. A statistically significant outcome is one that is unlikely to be due to chance alone, and this can be evaluated only under the condition of randomness. The conditions under which data are collected are important in drawing conclusions from the data; in critically reviewing uses of statistics in public media and other reports, it is important to consider the study design, how the data were gathered, and the analyses employed as well as the data summaries and the conclusions drawn.

Random processes can be described mathematically by using a probability model: a list or description of the possible outcomes (the sample space), each of which is assigned a probability. In situations such as flipping a coin, rolling a number cube, or drawing a card, it might be reasonable to assume various outcomes are equally likely. In a probability model, sample points represent outcomes and combine to make up events; probabilities of events can be computed by applying the Addition and Multiplication Rules. Interpreting these probabilities relies on an understanding of independence and conditional probability, which can be approached through the analysis of two-way tables.

Technology plays an important role in statistics and probability by making it possible to generate plots, regression functions, and correlation coefficients, and to simulate many possible outcomes in a short amount of time.

**Connections to Functions and Modeling**. Functions may be used to describe data; if the data suggest a linear relationship, the relationship can be modeled with a regression line, and its strength and direction can be expressed through a correlation coefficient.

**Conditional Probability and the Rules of Probability S.CP**

**Understand independence and conditional probability and use them to interpret data**

**MGSE9-12.S.CP.1** Describe categories of events as subsets of a sample space using unions, intersections, or complements of other events (*or, and, not*).

**MGSE9-12.S.CP.2** Understand that if two events A and B are independent, the probability of A and B occurring together is the product of their probabilities, and that if the probability of two events A and B occurring together is the product of their probabilities, the two events are independent.

**MGSE9-12.S.CP.3** Understand the conditional probability of A given B as P (A and B)/P(B). Interpret independence of A and B in terms of conditional probability; that is, the conditional probability of A given B is the same as the probability of A, and the conditional probability of B given A is the same as the probability of B.

**MGSE9-12.S.CP.4** Construct and interpret two-way frequency tables of data when two categories are associated with each object being classified. Use the two-way table as a sample space to decide if events are independent and to approximate conditional probabilities. *For example, use collected data from a random sample of students in your school on their favorite subject among math, science, and English. Estimate the probability that a randomly selected student from your school will favor science given that the student is in tenth grade. Do the same for other subjects and compare the results*.

**MGSE9-12.S.CP.5** Recognize and explain the concepts of conditional probability and independence in everyday language and everyday situations. *For example, compare the chance of having lung cancer if you are a smoker with the chance of being a smoker if you have lung cancer.*

**Use the rules of probability to compute probabilities of compound events in a uniform probability model**

**MGSE9-12.S.CP.6** Find the conditional probability of A given B as the fraction of B’s outcomes that also belong to A, and interpret the answer in context.

**MGSE9-12.S.CP.7** Apply the Addition Rule, P(A or B) = P(A) + P(B) – P(A and B), and interpret the answers in context.

**Mathematics | Standards for Mathematical Practice**

*Mathematical Practices are listed with each grade’s mathematical content standards to reflect the need to connect the mathematical practices to mathematical content in instruction.*

The Standards for Mathematical Practice describe varieties of expertise that mathematics educators at all levels should seek to develop in their students. These practices rest on important “processes and proficiencies” with longstanding importance in mathematics education. The first of these are the NCTM process standards of problem solving, reasoning and proof, communication, representation, and connections. The second are the strands of mathematical proficiency specified in the National Research Council’s report Adding It Up: adaptive reasoning, strategic competence, conceptual understanding (comprehension of mathematical concepts, operations and relations), procedural fluency (skill in carrying out procedures flexibly, accurately, efficiently and appropriately), and productive disposition (habitual inclination to see mathematics as sensible, useful, and worthwhile, coupled with a belief in diligence and one’s own efficacy).

**1 Make sense of problems and persevere in solving them.**

High school students start to examine problems by explaining to themselves the meaning of a problem and looking for entry points to its solution. They analyze givens, constraints, relationships, and goals. They make conjectures about the form and meaning of the solution and plan a solution pathway rather than simply jumping into a solution attempt. They consider analogous problems, and try special cases and simpler forms of the original problem in order to gain insight into its solution. They monitor and evaluate their progress and change course if necessary. Older students might, depending on the context of the problem, transform algebraic expressions or change the viewing window on their graphing calculator to get the information they need. By high school, students can explain correspondences between equations, verbal descriptions, tables, and graphs or draw diagrams of important features and relationships, graph data, and search for regularity or trends. They check their answers to problems using different methods and continually ask themselves, “Does this make sense?” They can understand the approaches of others to solving complex problems and identify correspondences between different approaches.

**2 Reason abstractly and quantitatively.**

High school students seek to make sense of quantities and their relationships in problem situations. They abstract a given situation and represent it symbolically, manipulate the representing symbols, and pause as needed during the manipulation process in order to probe into the referents for the symbols involved. Students use quantitative reasoning to create coherent representations of the problem at hand; consider the units involved; attend to the meaning of quantities, not just how to compute them; and know and flexibly use different properties of operations and objects.

**3 Construct viable arguments and critique the reasoning of others.**

High school students understand and use stated assumptions, definitions, and previously established results in constructing arguments. They make conjectures and build a logical progression of statements to explore the truth of their conjectures. They are able to analyze situations by breaking them into cases, and can recognize and use counterexamples. They justify their conclusions, communicate them to others, and respond to the arguments of others. They reason inductively about data, making plausible arguments that take into account the context from which the data arose. High school students are also able to compare the effectiveness of two plausible arguments, distinguish correct logic or reasoning from that which is flawed, and—if there is a flaw in an argument—explain what it is. High school students learn to determine domains to which an argument applies, listen or read the arguments of others, decide whether they make sense, and ask useful questions to clarify or improve the arguments.

**4 Model with mathematics.**

High school students can apply the mathematics they know to solve problems arising in everyday life, society, and the workplace. By high school, a student might use geometry to solve a design problem or use a function to describe how one quantity of interest depends on another. High school students making assumptions and approximations to simplify a complicated situation, realizing that these may need revision later. They are able to identify important quantities in a practical situation and map their relationships using such tools as diagrams, two-way tables, graphs, flowcharts and formulas. They can analyze those relationships mathematically to draw conclusions. They routinely interpret their mathematical results in the context of the situation and reflect on whether the results make sense, possibly improving the model if it has not served its purpose.

**5 Use appropriate tools strategically.**

High school students consider the available tools when solving a mathematical problem. These tools might include pencil and paper, concrete models, a ruler, a protractor, a calculator, a spreadsheet, a computer algebra system, a statistical package, or dynamic geometry software. High school students should be sufficiently familiar with tools appropriate for their grade or course to make sound decisions about when each of these tools might be helpful, recognizing both the insight to be gained and their limitations. For example, high school students analyze graphs of functions and solutions generated using a graphing calculator. They detect possible errors by strategically using estimation and other mathematical knowledge. When making mathematical models, they know that technology can enable them to visualize the results of varying assumptions, explore consequences, and compare predictions with data. They are able to identify relevant external mathematical resources, such as digital content located on a website, and use them to pose or solve problems. They are able to use technological tools to explore and deepen their understanding of concepts.

**6 Attend to precision.**

High school students try to communicate precisely to others by using clear definitions in discussion with others and in their own reasoning. They state the meaning of the symbols they choose, specifying units of measure, and labeling axes to clarify the correspondence with quantities in a problem. They calculate accurately and efficiently, express numerical answers with a degree of precision appropriate for the problem context. By the time they reach high school they have learned to examine claims and make explicit use of definitions.

**7 Look for and make use of structure.** By high school, students look closely to discern a pattern or structure. In the expression x2 + 9x + 14, older students can see the 14 as 2 × 7 and the 9 as 2 + 7. They recognize the significance of an existing line in a geometric figure and can use the strategy of drawing an auxiliary line for solving problems. They also can step back for an overview and shift perspective. They can see complicated things, such as some algebraic expressions, as single objects or as being composed of several objects. For example, they can see 5 – 3(x – y)2 as 5 minus a positive number times a square and use that to realize that its value cannot be more than 5 for any real numbers x and y. High school students use these patterns to create equivalent expressions, factor and solve equations, and compose functions, and transform figures.

**8 Look for and express regularity in repeated reasoning.**

High school students notice if calculations are repeated, and look both for general methods and for shortcuts. Noticing the regularity in the way terms cancel when expanding (x – 1)(x + 1), (x – 1)(x2 + x + 1), and (x – 1)(x3 + x2 + x + 1) might lead them to the general formula for the sum of a geometric series. As they work to solve a problem, derive formulas or make generalizations, high school students maintain oversight of the process, while attending to the details. They continually evaluate the reasonableness of their intermediate results.

# Connecting the Standards for Mathematical Practice to the Content Standards

The Standards for Mathematical Practice describe ways in which developing student practitioners of the discipline of mathematics increasingly ought to engage with the subject matter as they grow in mathematical maturity and expertise throughout the elementary, middle and high school years. Designers of curricula, assessments, and professional development should all attend to the need to connect the mathematical practices to mathematical content in mathematics instruction.

The Standards for Mathematical Content are a balanced combination of procedure and understanding. Expectations that begin with the word “understand” are often especially good opportunities to connect the practices to the content. Students who lack understanding of a topic may rely on procedures too heavily. Without a flexible base from which to work, they may be less likely to consider analogous problems, represent problems coherently, justify conclusions, apply the mathematics to practical situations, use technology mindfully to work with the mathematics, explain the mathematics accurately to other students, step back for an overview, or deviate from a known procedure to find a shortcut. In short, a lack of understanding effectively prevents a student from engaging in the mathematical practices.

In this respect, those content standards which set an expectation of understanding are potential “points of intersection” between the Standards for Mathematical Content and the Standards for Mathematical Practice. These points of intersection are intended to be weighted toward central and generative concepts in the school mathematics curriculum that most merit the time, resources, innovative energies, and focus necessary to qualitatively improve the curriculum, instruction, assessment, professional development, and student achievement in mathematics. See [Inside Math](http://www.insidemathematics.org/index.php/exemplary-lessons-integrating-practice-standards) for more resources.

# Classroom Routines

The importance of continuing the established classroom routines cannot be overstated. Daily routines must include such obvious activities as estimating, analyzing data, describing patterns, and answering daily questions. They should also include less obvious routines, such as how to select materials, how to use materials in a productive manner, how to put materials away, how to access classroom technology such as computers and calculators. An additional routine is to allow plenty of time for children to explore new materials before attempting any directed activity with these new materials.  The regular use of routines is important to the development of students' number sense, flexibility, fluency, collaborative skills and communication. These routines contribute to a rich, hands-on standards based classroom and will support students’ performances on the tasks in this unit and throughout the school year.

# Strategies for Teaching and Learning

* Students should be actively engaged by developing their own understanding.
* Mathematics should be represented in as many ways as possible by using graphs, tables, pictures, symbols and words.
* Interdisciplinary and cross curricular strategies should be used to reinforce and extend the learning activities.
* Appropriate manipulatives and technology should be used to enhance student learning.
* Students should be given opportunities to revise their work based on teacher feedback, peer feedback, and metacognition which includes self-assessment and reflection.
* Students should write about the mathematical ideas and concepts they are learning.
* Consideration of all students should be made during the planning and instruction of this unit. Teachers need to consider the following:
  + What level of support do my struggling students need in order to be successful with this unit?
  + In what way can I deepen the understanding of those students who are competent in this unit?
  + What real life connections can I make that will help my students utilize the skills practiced in this unit?

# Tasks

The framework tasks represent the level of depth, rigor, and complexity expected of all Geometry students. These tasks, or tasks of similar depth and rigor, should be used to demonstrate evidence of learning. It is important that all elements of a task be addressed throughout the learning process so that students understand what is expected of them. While some tasks are identified as a performance task, they may also be used for teaching and learning (learning/scaffolding task). The table below provides a brief explanation of the types of tasks that teachers will find in the frameworks units for Geometry.

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| --- | --- |
| **Scaffolding Task** | Tasks that build up to the learning task. |
| **Learning Task** | Constructing understanding through deep/rich contextualized problem solving tasks. |
| **Practice Task** | Tasks that provide students opportunities to practice skills and concepts. |
| **Performance Task** | Tasks which may be a formative or summative assessment that checks for student understanding/misunderstanding and or progress toward the standard/learning goals at different points during a unit of instruction. |
| **Culminating Task** | Designed to require students to use several concepts learned during the unit to answer a new or unique situation. Allows students to give evidence of their own understanding toward the mastery of the standard and requires them to extend their chain of mathematical reasoning. |
| **Short Cycle Task** | Designed to exemplify the performance targets that the standards imply. The tasks, with the associated guidance, equip teachers to monitor overall progress in their students’ mathematics. |
| **Formative Assessment Lesson (FAL)**  **\*more information on page 16** | Lessons that support teachers in formative assessment which both reveal and develop students’ understanding of key mathematical ideas and applications. These lessons enable teachers and students to monitor in more detail their progress towards the targets of the standards. |
| **3-Act Task**  **\*more information on page 18** | A Three-Act Task is a whole group mathematics task consisting of 3 distinct parts: an engaging and perplexing Act One, an information and solution seeking Act Two, and a solution discussion and solution revealing Act Three. |
| **Achieve CCSS- CTE Classroom Tasks** | Designed to demonstrate how the Common Core and Career and Technical Education knowledge and skills can be integrated. The tasks provide teachers with realistic applications that combine mathematics and CTE content. |

# Formative Assessment Lessons (FALs)

The **Formative** **Assessment Lesson** is designed to be part of an instructional unit typically implemented approximately two-thirds of the way through the instructional unit.  The results of the tasks should then be used to **inform** the instruction that will take place for the remainder of the unit.

Formative Assessment Lessons are intended to support teachers in formative assessment. They both reveal and develop students’ understanding of key mathematical ideas and applications. These lessons enable teachers and students to monitor in more detail their progress towards the targets of the standards. They assess students’ understanding of important concepts and problem solving performance, and help teachers and their students to work effectively together to move each student’s mathematical reasoning forward.

Videos of Georgia Teachers implementing FALs can be accessed [HERE](https://www.georgiastandards.org/Common-Core/Pages/Mathematics-Formative-Assessment-Lessons-Videos.aspx) and a sample of a FAL lesson may be seen [HERE](http://www.warrencountyschools.org/olc/page.aspx?id=78698&s=2608)

More information on types of Formative Assessment Lessons, their use, and their implementation may be found on the [Math Assessment Project](http://map.mathshell.org/guides/map_cc_teacher_guide.pdf)’s guide for teachers.

**Formative Assessment Lessons can also be found at the following sites:**[**Mathematics Assessment Project**](http://map.mathshell.org/materials/index.php)  
[**Kenton County Math Design Collaborative**](http://kentoncountymdc.wikispaces.com/home)[**MARS Tasks by grade level**](http://scoe.org/pub/htdocs/ccss-mathematics.html)

A **sample FAL** with extensive dialog and suggestions for teachers may be found [HERE](https://www.google.com/url?sa=t&rct=j&q=&esrc=s&source=web&cd=6&cad=rja&ved=0CFIQFjAF&url=http%3A%2F%2Feducore.ascd.org%2Fresource%2Fdownload%2Fget.ashx%3Fguid%3De35ed6b7-cf7c-49e8-87b0-d79994d4e743&ei=SfmtUazaBIr29gSjmIHAAw&usg=AFQjCNEsXL0KLdKdHTTPMLZvEZ5efSfjjQ). This resource will help teachers understand the flow and purpose of a FAL.

The [**Math Assessment Project**](http://map.mathshell.org/materials/index.php?subpage=about) has developed Professional Development Modules that are designed to help teachers with the practical and pedagogical challenges presented by these lessons.

[Module 1](http://map.mathshell.org/static/draft/pd/modules/1_Formative_Assessment/html/index.htm) introduces the model of *formative assessment* used in the lessons, its theoretical background and practical implementation. [Modules 2](http://map.mathshell.org/static/draft/pd/modules/2_Concept_Lessons/html/index.htm) & [3](http://map.mathshell.org/static/draft/pd/modules/3_Problem_Solving/html/index.htm) look at the two types of Classroom Challenges in detail. [Modules 4](http://map.mathshell.org/static/draft/pd/modules/4_Questioning/html/index.htm) & [5](http://map.mathshell.org/static/draft/pd/modules/5_Collaborative_work/html/index.htm) explore two crucial pedagogical features of the lessons: asking probing questions and collaborative learning.

Georgia RESA’s may be contacted about professional development on the use of FALs in the classroom. The request should be made through the teacher's local RESA and can be referenced by asking for more information on the Mathematics Design Collaborative (MDC).

# Spotlight Tasks

A Spotlight Task has been added to each GSE mathematics unit in the Georgia resources for middle and high school.  The Spotlight Tasks serve as exemplars for the use of the Standards for Mathematical Practice, appropriate unit-level Georgia Standards of Excellence, and research-based pedagogical strategies for instruction and engagement. Each task includes teacher commentary and support for classroom implementation.  Some of the Spotlight Tasks are revisions of existing Georgia tasks and some are newly created.  Additionally, some of the Spotlight Tasks are 3-Act Tasks based on 3-Act Problems from Dan Meyer and Problem-Based Learning from Robert Kaplinsky.

# 3-Act Tasks

A Three-Act Task is a whole group mathematics task consisting of 3 distinct parts: an engaging and perplexing Act One, an information and solution seeking Act Two, and a solution discussion and solution revealing Act Three.

**Guidelines for 3-Act Tasks and Patient Problem Solving (Teaching without the Textbook)**

*Adapted from Dan Meyer*

**Developing the mathematical Big Idea behind the 3-Act task:**

* Create or find/use a clear visual which tells a brief, perplexing mathematical story. Video or live action works best. (See resource suggestions in the Guide to 3-Act Tasks)
* Video/visual should be real life and allow students to see the situation unfolding.
* Remove the initial literacy/mathematics concerns. Make as few language and/or math demands on students as possible. You are posing a mathematical question without words.
* The visual/video should inspire curiosity or perplexity which will be resolved via the mathematical big idea(s) used by students to answer their questions. You are creating an intellectual need or cognitive dissonance in students.

**Enacting the 3-Act in the Classroom**

**Act 1 (The Question):**

Set up student curiosity by sharing a scenario:

* Teacher says, “I’m going show you something I came across and found interesting” or, “Watch this.”
* Show video/visual.
* Teacher asks, “What do you notice/wonder?” and “What are the first questions that come to mind?”
* Students share observations/questions with a partner first, then with the class (Think-Pair-Share). Students have ownership of the questions because they posed them.
* Leave no student out of this questioning. Every student should have access to the scenario. No language or mathematical barriers. Low barrier to entry.
* Teacher records questions (on chart paper or digitally-visible to class) and ranks them by popularity.
* Determine which question(s) will be immediately pursued by the class. If you have a particular question in mind, and it isn’t posed by students, you may have to do some skillful prompting to orient their question to serve the mathematical end. However, a good video should naturally lead to the question you hope they’ll ask. You may wish to pilot your video on colleagues before showing it to students. If they don’t ask the question you are after, your video may need some work.
* Teacher asks for estimated answers in response to the question(s). Ask first for best estimates, then request estimates which are too high and too low. Students are no defining and defending parameters for making sense of forthcoming answers.
* Teacher asks students to record their actual estimation for future reference.

**Act 2 (Information Gathering):**

Students gather information, draw on mathematical knowledge, understanding, and resources to answer the big question(s) from Act-1:

* Teacher asks, “What information do you need to answer our *main question*?”
* Students think of the important information they will need to answer their questions.
* Ask, “What mathematical tools do you have already at your disposal which would be useful in answering this question?”
* What mathematical tools might be useful which students don’t already have? Help them develop those.
* Teacher offers smaller examples and asks probing questions.
  + What are you doing?
  + Why are you doing that?
  + What would happen if…?
  + Are you sure? How do you know?

**Act 3 (The Reveal):**

The payoff.

* Teacher shows the answer and validates students’ solutions/answer.
* Teacher revisits estimates and determines closest estimate.
* Teacher compares techniques, and allows students to determine which is most efficient.

**The Sequel:**

* Students/teacher generalize the math to any case, and “algebrafy” the problem.
* Teacher poses an extension problem- best chance of student engagement if this extension connects to one of the many questions posed by students which were not the focus of Act 2, or is related to class discussion generated during Act 2.
* Teacher revisits or reintroduces student questions that were not addressed in Act 2.

# Why Use 3-Act Tasks? A Teacher’s Response

The short answer:  It's what's best for kids!

If you want more, read on:

The need for students to make sense of problems can be addressed through tasks like these.  The challenge for teachers is, to quote [Dan Meyer](https://www.ted.com/talks/dan_meyer_math_curriculum_makeover), “be less helpful.”  (To clarify, being less helpful means to first allow students to generate questions they have about the picture or video they see in the first act, then give them information as they ask for it in act 2.)  Less helpful does not mean give these tasks to students blindly, without support of any kind!

This entire process will likely cause some anxiety (for all).  When jumping into 3-Act tasks for the first (second, third, . . .) time, students may not generate the suggested question.  As a matter of fact, in this task about [proportions and scale](http://mikewiernicki3act.wordpress.com/sphero-draw-drive/), students may ask many questions that are curious questions, but have nothing to do with the mathematics you want them to investigate.  One question might be “How is that ball moving by itself?”  It’s important to record these and all other questions generated by students.  This validates students' ideas.  Over time, students will become accustomed to the routine of 3-act tasks and come to appreciate that there are certain kinds of mathematically answerable questions – most often related to quantity or measurement.

These kinds of tasks take time, practice and patience.  When presented with options to use problems like this with students, the easy thing for teachers to do is to set them aside for any number of "reasons."  I've highlighted a few common "reasons" below with my commentary (in blue):

* This will take too long.  I have a lot of content to cover.  (Teaching students to think and reason is embedded in mathematical content at all levels - how can you **not** take this time)
* They need to be taught the skills first, then maybe I’ll try it.  (An important part of learning mathematics lies in productive struggle and learning to persevere [SMP 1].  What better way to discern what students know and are able to do than with a mathematical context [problem] that lets them show you, based on the knowledge they already have - prior to any new information. To quote John Van de Walle, “Believe in kids and they will, flat out, amaze you!”)
* My students can’t do this.  (Remember, whether you think they can or they can’t, you’re right!)  (Also, this expectation of students persevering and solving problems is in every state's standards - and was there even before Georgia Standards of Excellence!)
* I'm giving up some control.  (Yes, and this is a bit scary.  You're empowering students to think and take charge of their learning.  So, what can you do to make this *less* scary? **Do what we expect students to do:**
  + Persevere.  Keep trying these and other open-beginning, -middle, and -ended problems.  Take note of what's working and focus on it!
  + Talk with a colleague (work with a partner).  Find that critical friend at school, another school, online. . .
  + Question (use #MTBoS on Twitter, or blogs, or Google: 3-act tasks).

The benefits of students learning to question, persevere, problem solve, and reason mathematically far outweigh any of the reasons (read excuses) above.  The time spent up front, teaching through tasks such as these and other open problems, creates a huge pay-off later on.  However, it is important to note, that the problems themselves are worth nothing without teachers setting the expectation that students:  question, persevere, problem solve, and reason mathematically on a daily basis.  Expecting these from students, and facilitating the training of how to do this consistently and with fidelity is principal to success for both students and teachers.

Yes, all of this takes time.  For most of my classes, mid to late September (we start school at the beginning of August) is when students start to become comfortable with what problem solving really is.  It's not word problems - mostly. It's not the problem set you do after the skill practice in the textbook.  Problem solving is what you do when you don't know what to do!  This is difficult to teach kids and it does take time.  But it is worth it!  More on this in a future blog!

**Tips:**

One strategy I've found that really helps students generate questions is to allow them to talk to their peers about what they notice and wonder first (Act 1).  Students of all ages will be more likely to share once they have shared and tested their ideas with their peers.  This does take time.  As you do more of these types of problems, students will become familiar with the format and their comfort level may allow you to cut the amount of peer sharing time down before group sharing.

What do you do if they don’t generate the question suggested?  Well, there are several ways that this can be handled.  If students generate a similar question, use it.  Allowing students to struggle through their question and ask for information is one of the big ideas here.  Sometimes, students realize that they may need to solve a different problem before they can actually find what they want.  If students are way off, in their questions, teachers can direct students, carefully, by saying something like:  “You all have generated some interesting questions.  I’m not sure how many we can answer in this class.  Do you think there’s a question we could find that would allow us to use our knowledge of mathematics to find the answer to (insert quantity or measurement)?”  Or, if they are really struggling, you can, again carefully, say “You know, I gave this problem to a class last year (or class, period, etc) and they asked (insert something similar to the suggested question here).  What do you think about that?”  Be sure to allow students to share their thoughts.

After solving the main question, if there are other questions that have been generated by students, it’s important to allow students to investigate these as well.  Investigating these additional questions validates students’ ideas and questions and builds a trusting, collaborative learning relationship between students and the teacher.

Overall, we're trying to help our students mathematize their world.  We're best able to do that when we use situations that are relevant (no dog bandanas, please), engaging (create an intellectual need to know), and perplexing.  If we continue to use textbook type problems that are too helpful, uninteresting, and let's face it, perplexing in all the wrong ways, we're not doing what's best for kids; we're training them to not be curious, not think, and worst of all . . . dislike math.

**3-Act Task Resources**:

* [www.estimation180.com](https://mikewiernicki.wordpress.com/wp-admin/www.estimation180.com)
* [www.visualpatterns.org](https://mikewiernicki.wordpress.com/wp-admin/www.visualpatterns.org)
* [101 Questions](http://www.101qs.com/)
* [Dan Meyer's 3-Act Tasks](https://docs.google.com/spreadsheet/ccc?key=0AjIqyKM9d7ZYdEhtR3BJMmdBWnM2YWxWYVM1UWowTEE#gid=0)
* [3-Act Tasks for Elementary and Middle School](https://docs.google.com/spreadsheet/ccc?key=0Are6h0vMbntddGVlQkE2VzgyZkdJb3NBWWwtamhJQXc&usp=drive_web#gid=0)
* [Andrew Stadel](http://mr-stadel.blogspot.com/)
* [Jenise Sexton](http://doesthismake.blogspot.com/)
* [Graham Fletcher](http://gfletchy.wordpress.com/)
* [Fawn Nguyen](http://fawnnguyen.com/)
* [Robert Kaplinsky](http://robertkaplinsky.com/)
* [Open Middle](http://www.openmiddle.com/)
* Check out the Math Twitter Blog-o-Sphere (MTBoS) - you’ll find tons of support and ideas!

# Assessment Resources and Instructional Support Resources

The resource sites listed below are provided by the GADOE and are designed to support the instructional and assessment needs of teachers. All BLUE links will direct teachers to the site mentioned.

* [Georgiastandards.org](https://www.georgiastandards.org/Pages/Default.aspx) provides a gateway to a wealth of instructional links and information. Select the ELA/Math tab at the top to access specific math resources for GSE.
* MGSE Frameworks are "models of instruction" designed to support teachers in the implementation of the Georgia Standards of Excellence (GSE).  The Georgia Department of Education, Office of Standards, Instruction, and Assessment has provided an example of the Curriculum Map for each grade level and examples of Frameworks aligned with the GSE to illustrate what can be implemented within the grade level. School systems and teachers are free to use these models as is; modify them to better serve classroom needs; or create their own curriculum maps, units and tasks. [<http://bit.ly/1AJddmx>](https://www.georgiastandards.org/Common-Core/Pages/Math.aspx)
* [The Teacher Resource Link](http://www.gadoe.org/Technology-Services/Instructional-Technology/Pages/Teacher-Resource-Link.aspx) (TRL) is an application that delivers vetted and aligned digital resources to Georgia’s teachers. TRL is accessible via the GADOE “tunnel” in conjunction with SLDS using the single sign-on process. The content is pushed to teachers based on course schedule.
* [Georgia Virtual School](http://www.gavirtuallearning.org/Resources.aspx) content available on our Shared Resources Website is available for anyone to view.  Courses are divided into modules and are aligned with the Georgia Standards of Excellence.
* The Georgia Online Formative Assessment Resource (GOFAR) accessible through SLDS contains test items related to content areas assessed by the Georgia Milestones Assessment System and NAEP.  Teachers and administrators can utilize the GOFAR to develop formative and summative assessments, aligned to the state-adopted content standards, to assist in informing daily instruction.

The Georgia Online Formative Assessment Resource (GOFAR) provides the ability for Districts and Schools to assign benchmark and formative test items/tests to students in order to obtain information about student progress and instructional practice. GOFAR allows educators and their students to have access to a variety of test items – selected response and constructed response – that are aligned to the State-adopted content standards for Georgia’s elementary, middle, and high schools.

Students, staff, and classes are prepopulated and maintained through the State Longitudinal Data System (SLDS).  Teachers and Administrators may view Exemplars and Rubrics in Item Preview. A scoring code may be distributed at a local level to help score constructed response items.

For GOFAR user guides and overview, please visit:

<https://www.gadoe.org/Curriculum-Instruction-and-Assessment/Assessment/Pages/Georgia-Online-Formative-Assessment-Resource.aspx>

* [Course/Grade Level WIKI](http://ccgpsmathematics9-10.wikispaces.com/home) spaces are available to post questions about a unit, a standard, the course, or any other GSE math related concern.  Shared resources and information are also available at the site.
* Georgia Milestones Assessment System resources can be found at:<http://www.gadoe.org/Curriculum-Instruction-and-Assessment/Assessment/Pages/Georgia-Milestones-Assessment-System.aspx>

Features the Georgia Milestones Assessment System include:

o   Open-ended (constructed-response) items

* + Norm-referenced to complement the criterion-referenced information and to provide a national comparison;
  + Transition to online administration over time, with online administration considered the primary mode of administration and paper-penc​il as back-up until the transition is complete.

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| Internet Resources |

The following list is provided as a sample of available resources and is for informational purposes only. It is your responsibility to investigate them to determine their value and appropriateness for your district. GADOE does not endorse or recommend the purchase of or use of any particular resource.

**General Resources**

[Illustrative Mathematics](http://www.illustrativemathematics.org)

Standards are illustrated with instructional and assessment tasks, lesson plans, and other curriculum resources.

[Mathematics in Movies](http://www.math.harvard.edu/~knill/mathmovies/)

Short movie clips related to a variety of math topics.

[Mathematical Fiction](http://kasmana.people.cofc.edu/MATHFICT/browse.php)

Plays, short stories, comic books and novels dealing with math.

[The Shodor Educational Foundation](http://www.shodor.org/interactivate/lessons/byAudience/)

This website has extensive notes, lesson plans and applets aligned with the standards.

[NEA Portal Arkansas Video Lessons on-line](http://neaportal.k12.ar.us/index.php/9th-12th-grades-mathematics/)

The NEA portal has short videos aligned to each standard. This resource may be very helpful for students who need review at home.

[Learnzillion](http://learnzillion.com/common_core/math/hs)

This is another good resource for parents and students who need a refresher on topics.

[Math Words](http://www.mathwords.com/)

This is a good reference for math terms.

[National Library of Virtual Manipulatives](http://nlvm.usu.edu/en/nav/vlibrary.html) Java must be enabled for this applet to run. This website has a wealth of virtual manipulatives helpful for use in presentation. The resources are listed by domain.

[Geogebra Download](http://www.geogebra.org/cms/download)

Free software similar to Geometer’s Sketchpad. This program has applications for algebra, geometry, and statistics.

[Utah Resources](http://www.uen.org/k12educator/uenresources.php?cat=Mathematics)

Open resource created by the Utah Education Network.

**Resources for Problem-based Learning**

[Dan Meyer’s Website](http://blog.mrmeyer.com/)

Dan Meyer has created many problem-based learning tasks. The tasks have great hooks for the students and are aligned to the standards in this [spreadsheet](https://docs.google.com/spreadsheet/ccc?key=0AjIqyKM9d7ZYdEhtR3BJMmdBWnM2YWxWYVM1UWowTEE#gid=0).

[Andrew Stadel](https://docs.google.com/spreadsheet/ccc?key=0AkLk45wwjYBudG9LeXRad0lHM0E0VFRyOEtRckVvM1E#gid=0)

Andrew Stadel has created many problem-based learning tasks using the same format as Dan Meyer.

[Robert Kaplinsky](http://robertkaplinsky.com/lessons/)

Robert Kaplinsky has created many tasks that engage students with real life situations.

[Geoff Krall’s Emergent Math](http://emergentmath.com/my-problem-based-curriculum-maps/)

Geoff Krall has created a curriculum map structured around problem-based learning tasks.